

Suppose vacuum permittivity and permeability are  $\epsilon_0$  and  $\mu_0$  respectively.

- (1) The capacitance per length is  $C' = \epsilon_0 \frac{w}{d}$ , the inductance per length is  $L' = \mu_0 \frac{d}{w}$ . Then the

$$\text{characteristic impedance is } Z_0 = \sqrt{\frac{L'}{C'}} = \sqrt{\frac{\mu_0}{\epsilon_0} \frac{d}{w}} = 94.25 \Omega.$$

The wavelength is  $\lambda = \frac{c}{f} = 0.1667 \text{ m}$ , the wavenumber is  $\beta = \frac{2\pi}{\lambda} = 37.7 / \text{m}$ . The phase

velocity is  $u_p = c = 3 \times 10^8 \text{ m/s}$ .

- (2) The general phasor forms are:

$$\begin{cases} \tilde{V}(z) = |V_0^+| e^{j\phi^+} e^{-j\beta z} + |V_0^-| e^{j\phi^-} e^{j\beta z} \\ \tilde{I}(z) = \frac{|V_0^+| e^{j\phi^+} e^{-j\beta z}}{Z_0} - \frac{|V_0^-| e^{j\phi^-} e^{j\beta z}}{Z_0}, \end{cases}$$

which in the time domain are

$$\begin{cases} V(z, t) = |V_0^+| \cos(\omega t - \beta z + \phi^+) + |V_0^-| \cos(\omega t + \beta z + \phi^-) \\ I(z, t) = \frac{|V_0^+| \cos(\omega t - \beta z + \phi^+)}{Z_0} - \frac{|V_0^-| \cos(\omega t + \beta z + \phi^-)}{Z_0} \end{cases}$$

- (3) The reflection coefficient at  $z = 0$  is  $\Gamma = \frac{Z_L - Z_0}{Z_L + Z_0} = 1$ , where  $Z_L = \infty$  is the open-circuited

impedance. The current at  $z = 0$  must be zero, i.e.  $\tilde{I}(0) = 0$ .

- (4) The reflection coefficient  $\Gamma(z) = \Gamma e^{-j2\beta z}$ , then the reflection coefficient at  $z = z_1$  is

$$\Gamma(z) = \Gamma e^{-j2\beta z_1} = e^{-j0.72\pi}.$$

- (5) Since the transmission line is open-circuited, the current at  $z = 0$  is zero. Then the phasor forms are:

$$\begin{cases} \tilde{V}(z) = V_0^+ (e^{-j\beta z} + e^{j\beta z}) = 2V_0^+ \cos(\beta z) \\ \tilde{I}(z) = \frac{V_0^+}{Z_0} (e^{-j\beta z} - e^{j\beta z}) = -2jV_0^+ \sin(\beta z) \end{cases}$$

Using  $\tilde{I}(z_1) = 2e^{j\pi/4} A$ , we can calculate

$$\begin{cases} \tilde{V}(z) = 208 e^{j3\pi/4} \cos(\beta z) V \\ \tilde{I}(z) = 2.2 e^{j\pi/4} \sin(\beta z) A \end{cases}$$

It follows that  $\tilde{I}(0) = 0$ ,  $\tilde{V}(0) = 208.32 e^{j3\pi/4} V$ , and  $\tilde{V}(z_1) = 88.7 e^{j3\pi/4} V$ .